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ARTICLE

Thermodynamics of Reduction of Titania by CH₄-H₂ Gas Mixture

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Abstract: Given the considerable global interest in the preparation of Ti and TiC, a novel reduction method for TiO₂ in a CH₄-H₂ atmosphere was proposed, and the reduction thermodynamic behavior, phase equilibrium, and energy consumption of TiO₂ during its reaction with a CH₄-H₂ gas mixture were investigated. The results indicate that the reaction proceeds via a stepwise reduction pathway from TiO₂ to Ti(C, O), with the Magnéli phase (Ti_nO_{2n-1}) and Ti₃O₅ serving as intermediate phases. Notably, the reduction of TiO₂ by H₂ is more challenging than that by CH₄, which may be attributed to the inhibitory effect of H₂ on the surface carbon precipitation. For the complete carbonization of 1 mol TiO₂, the total energy required at 1000, 1100, and 1200 °C is 1159, 925, and 977 kJ/mol, respectively, which may be related to the shift of gas-phase equilibrium and the increase in side reactions at high temperatures.

Key words: TiO₂; TiC_xO_y; reduction-carbonization; thermodynamic behavior; energy consumption

1 Introduction

Titanium and its alloys are noted for their unique combination of properties, including high strength, low density, a high melting point, excellent corrosion resistance, and superior biocompatibility^[1-8], making them essential in aerospace, defense, biomedicine, and daily-life applications^[9-13]. The history of titanium metal preparation dates back to the 1910s, when Hunter synthesized Ti from TiCl₄ using sodium as a reductant in a steel reactor filled with argon gas^[14]. However, the early method for producing sponge titanium suffered from restrictions such as high impurity levels and low efficiency, leading to its replacement by the Kroll method, developed in the 1950s, which offered enhanced efficiency^[15-17]. The Kroll method involves two key steps: first, the carbothermal chlorination of TiO₂ to produce TiCl₄; second, the reaction of TiCl₄ with liquid Mg to yield metallic titanium. The resulting product then undergoes vacuum distillation to remove impurities, ultimately obtaining sponge titanium with low oxygen content^[18-19]. Despite cost reduction benefits, the Kroll method still faces challenges like high energy consump-

tion during the carbothermal chlorination step and equipment corrosion caused by chlorine gas at high temperatures^[20-22].

In titanium production, extensive efforts have been devoted to find more efficient processes than the Kroll method, aiming to lower costs and enhance energy efficiency. Researchers at Pangang Group Research Institute Co., Ltd have worked on titanium-containing blast furnace slag: they first generated TiC and TiC_xO_y via a carbothermal reaction; then, these products are subjected to selective chlorination to produce TiCl₄; finally, TiCl₄ was reduced to sponge titanium via a magnesiothermic process. This approach improves the utilization of low-grade titanium resources and lowers production costs^[23-24]. In the 1950s, the MER Corporation developed a process that uses cheap titanium feedstocks and a carbon composite anode. This process releases Ti ions into the electrolyte during electrolysis, and then they are deposited as solid Ti on the cathode^[25]. Later, in 1991, Popov et al^[26] used TiC as a consumable anode for the cathodic deposition of high-purity titanium; however, this method also generates Magnéli phases and carries the risk of carbon contamination

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in the final product. The USTB process, developed by the University of Science and Technology Beijing, starts by reducing TiO_2 with carbon to produce electrically conductive TiC_xO_y , which is then used as an anode in electrolysis to release low-valent Ti ions into the molten salt, ultimately forming pure Ti at the cathode^[27–28].

These innovative approaches, which use TiC and TiC_xO_y as raw materials for titanium production, demonstrate new advancements in the field towards cost reduction and efficiency enhancement. These methods not only lessen the environmental impact but also improve the production efficiency and quality of Ti materials. The primary method for producing TiC/ TiC_xO_y is the carbothermal reduction process, which employs TiO_2 powder and carbon powder as raw materials in a high-temperature argon atmosphere. Although this method is cost-effective and simple, it is associated with high energy consumption and substantial carbon emissions^[29]. Additionally, for the production of high-purity TiC, Feng et al^[30–31] suggested the synthesis of TiC nanoparticles through an 8 h reaction between TiCl_4 and CaC_2 at 500 °C under high-pressure conditions. Wang et al^[32] proposed a process that combines TiO_2 with $\text{CaC}_2/\text{NaNH}_2$, supplemented by metallic magnesium under high pressure, to produce TiC. These processes typically employ high-purity TiO_2 powder and TiCl_4 as raw materials, both of which are costly. Moreover, the complexity of these processes and the high energy consumption during production restrict their application to only the manufacturing of materials with specific requirements.

To address these challenges, a novel reduction approach using CH_4 is proposed as an alternative to traditional high-temperature carburization techniques. Previous research has demonstrated the successful synthesis of TiC using methane-bearing gas^[33–35]. Subsequently, an innovative process aimed at reducing TiO_2 with a $\text{CH}_4\text{-H}_2$ gas mixture has shown considerable potential advantages and has been deemed feasible, confirming that TiO_2 can be reduced and carbonized to Ti(C, O) under a $\text{CH}_4\text{-H}_2$ atmosphere at relatively low temperatures^[36–37]. However, the reduction products of TiO_2 reduced by H_2 and CH_4 are relatively complex, containing not only water and carbon dioxide but also solid solutions and low-valent titanium oxides. The formation of these products is influenced by system pressure, gas composition, and reaction temperature^[38–41]. Hence, the reactions between TiO_2 and the $\text{CH}_4\text{-H}_2$ gas mixture during the reduction process are markedly more complicated. To decipher the reaction stages and energy consumption of this novel process, this study explored the thermodynamic behavior of TiO_2 under a $\text{CH}_4\text{-H}_2$ atmosphere and estimated the reaction enthalpy changes.

2 Experiment

2.1 Equilibrium composition calculation settings

The thermodynamic equilibrium and Gibbs free energy changes associated with the reduction of TiO_2 by a $\text{CH}_4\text{-H}_2$ gas mixture were calculated using FactSage 8.0, with the FactPS and FToxid databases used as data support. Initially, the

reaction module was employed to compute all potential reactions between TiO_2 and the $\text{CH}_4\text{-H}_2$ gas mixture, with the consideration of the effects of different reaction pressures. Subsequently, the thermodynamic equilibrium of the system under various temperatures was determined using the equilibrium module, which is based on the principle of minimum Gibbs free energy. Additionally, the phase diagram module was used to generate the phase diagrams that illustrate the evolution of TiO_2 behavior with varying gas composition.

The initial and equilibrium states of the system are depicted in Fig. 1, while the initial gas volume fraction is detailed in Table 1. The reaction system contains both solid and gaseous phases. The reaction temperatures were set in the range from 900 °C to 1200 °C at intervals of 100 °C. The system pressure was maintained constant before and after the reaction. To ensure the complete reduction and carbonization of TiO_2 , the total reaction gas volume was set at 50 mol.

In practical industrial scenarios, a piston flow reactor configuration is often employed, where the reaction gas and solid reactants flow in countercurrent directions. This design enables the spent gas to rapidly depart from the reaction interface, while fresh reaction gas is immediately supplied to the interface. Thermodynamic calculations were conducted for an open system to determine the phase transformations and solid-phase composition. The reaction process was simulated through 1000 reaction steps, with each step introducing a fresh batch of 0.05 mol reaction gas.

2.2 Calculation of reaction enthalpy

The thermodynamic equilibrium of TiO_2 reacting with a $\text{CH}_4\text{-H}_2$ gas mixture was assessed in an open system to derive crucial information, including the composition of solid products and off-gas, along with the required amount of reducing gas. Based on these results, the change in reaction enthalpy was determined, which stemmed from the disparity

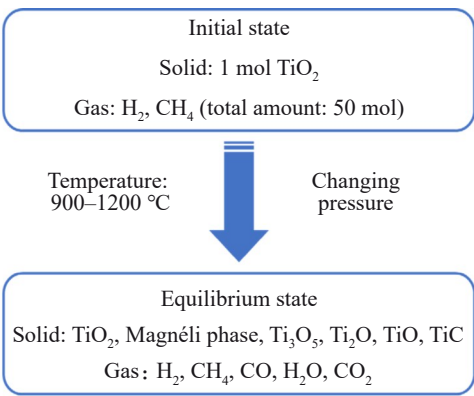


Fig.1 Initial and equilibrium states of reaction system

Table 1 Contents of initial reaction gases (vol%)

Order	CH ₄	H ₂	Total
(1)	4	96	100
(2)	8	92	100
(3)	12	88	100
(4)	16	84	100

in absolute enthalpy between reactants and products.

The enthalpy of a substance at a given state is an absolute value, which is derived from the fundamental data of ΔH_{298} and $C_p(T)$, as illustrated in Eq.(1–2).

$$H_T = \Delta H_{298} + \int_{298}^T C_p(T) dT \quad (1)$$

$$C_p(T) = A_1 + A_2 \times 10^{-3}T + A_3 \times 10^5 T^{-2} + A_4 \times 10^{-6}T \quad (2)$$

where $C_p(T)$ denotes the isobaric molar heat capacity at a specific temperature T , with the unit of J/(mol·K); H_T denotes the standard molar enthalpy at temperature T , with the unit of J/mol; A_1 , A_2 , A_3 , and A_4 are parameters characterizing the specific heat capacity; ΔH_{298} denotes the standard enthalpy change for formation of each substance at 298 K.

The enthalpy change of a chemical reaction denotes the heat absorbed or released by the system when the reaction reaches equilibrium. It is calculated as the difference between the total enthalpies of the products and those of the reactants, as delineated in Eq.(3).

$$\Delta H = \sum_{i=1}^N n_i H_{i,T_i} - \sum_{j=1}^M n_j H_{j,T_j} \quad (3)$$

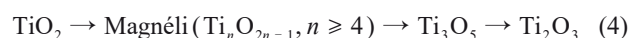
where ΔH denotes the enthalpy change of reactions (kJ/mol), with a negative value indicating the exothermic reaction and a positive value indicating the endothermic reaction; indices i and j represent the components after and before the state change, respectively; N and M denote the number of components after and before the state change, respectively; n_i and n_j are the molar amounts of the components after and before the state change, respectively, with the unit of mol; T_i and T_j signify the thermodynamic temperatures of the components after and before the state change, respectively,

and their units are K. The standard molar enthalpy of component i at temperature T_i and that of component j at temperature T_j are represented as $H_i^0(T_i)$ and $H_j^0(T_j)$, respectively, with the unit of kJ/mol.

3 Results and Discussion

3.1 Gibbs free energy change of reactions

The reduction and carbonization of TiO_2 is regarded as a stepwise process, with the phase transition sequence given as follows^[42]:



The reaction of an ideal gas can be described by the following equation:



The Gibbs free energy change ΔG of this reaction is calculated by the following equation:

$$\Delta G = \Delta G^0 + \ln \left(\frac{p_D^d p_H^h}{p_A^a p_B^b} p^{\Theta \sum v_i} \right) \quad (6)$$

where ΔG^0 indicates the standard Gibbs free energy change. When the reaction gas is at standard atmospheric pressure, the following relationship holds:

$$\Delta G = \Delta G^0 \quad (7)$$

The possible reactions of TiO_2 with CH_4 and H_2 are listed in Table 2. The Gibbs free energy changes of TiO_2 in the presence of a CH_4 - H_2 gas mixture were calculated using the Reaction Module of FactSage. Additionally, the relationship between Gibbs free energy changes and temperature, as well as the initial reaction temperature (T_{initial}) for each reaction, are identified and also shown in Table 2. The thermodynamic data

Table 2 Possible reactions of TiO_2 with CH_4 and H_2

Reaction	Equation	$\Delta G^0/\text{kJ} \cdot \text{mol}^{-1}$	$T_{\text{initial}}/\text{K}$
$20\text{TiO}_2 + \text{H}_2 = \text{Ti}_{20}\text{O}_{39} + \text{H}_2\text{O}$	Eq.(8)	$120.446 - 0.063T$	1919
$20\text{TiO}_2 + \text{CH}_4 = \text{Ti}_{20}\text{O}_{39} + \text{CO} + 2\text{H}_2$	Eq.(9)	$343.038 - 0.314T$	1093
$10\text{TiO}_2 + \text{H}_2 = \text{Ti}_{10}\text{O}_{19} + \text{H}_2\text{O}$	Eq.(10)	$120.007 - 0.057T$	2088
$10\text{TiO}_2 + \text{CH}_4 = \text{Ti}_{10}\text{O}_{19} + \text{CO} + 2\text{H}_2$	Eq.(11)	$342.663 - 0.309T$	1111
$9\text{TiO}_2 + \text{H}_2 = \text{Ti}_9\text{O}_{17} + \text{H}_2\text{O}$	Eq.(12)	$119.993 - 0.057T$	2112
$9\text{TiO}_2 + \text{CH}_4 = \text{Ti}_9\text{O}_{17} + \text{CO} + 2\text{H}_2$	Eq.(13)	$342.584 - 0.308T$	1112
$8\text{TiO}_2 + \text{H}_2 = \text{Ti}_8\text{O}_{15} + \text{H}_2\text{O}$	Eq.(14)	$120.002 - 0.056T$	2140
$8\text{TiO}_2 + \text{CH}_4 = \text{Ti}_8\text{O}_{15} + \text{CO} + 2\text{H}_2$	Eq.(15)	$342.594 - 0.307T$	1115
$7\text{TiO}_2 + \text{H}_2 = \text{Ti}_7\text{O}_{13} + \text{H}_2\text{O}$	Eq.(16)	$120.146 - 0.055T$	2173
$7\text{TiO}_2 + \text{CH}_4 = \text{Ti}_7\text{O}_{13} + \text{CO} + 2\text{H}_2$	Eq.(17)	$342.737 - 0.307T$	1119
$6\text{TiO}_2 + \text{H}_2 = \text{Ti}_6\text{O}_{11} + \text{H}_2\text{O}$	Eq.(18)	$120.506 - 0.054T$	2218
$6\text{TiO}_2 + \text{CH}_4 = \text{Ti}_6\text{O}_{11} + \text{CO} + 2\text{H}_2$	Eq.(19)	$343.097 - 0.305T$	1123
$5\text{TiO}_2 + \text{H}_2 = \text{Ti}_5\text{O}_9 + \text{H}_2\text{O}$	Eq.(20)	$121.316 - 0.053T$	2278
$5\text{TiO}_2 + \text{CH}_4 = \text{Ti}_5\text{O}_9 + \text{CO} + 2\text{H}_2$	Eq.(21)	$343.908 - 0.304T$	1130
$4\text{TiO}_2 + \text{H}_2 = \text{Ti}_4\text{O}_7 + \text{H}_2\text{O}$	Eq.(22)	$123.168 - 0.052T$	2360
$4\text{TiO}_2 + \text{CH}_4 = \text{Ti}_4\text{O}_7 + \text{CO} + 2\text{H}_2$	Eq.(23)	$345.759 - 0.303T$	1140
$3\text{Ti}_4\text{O}_7 + \text{H}_2 = 4\text{Ti}_3\text{O}_5 + \text{H}_2\text{O}$	Eq.(24)	$172.077 - 0.071T$	2427
$3\text{Ti}_4\text{O}_7 + \text{CH}_4 = 4\text{Ti}_3\text{O}_5 + \text{CO} + 2\text{H}_2$	Eq.(25)	$393.339 - 0.323T$	1218
$2\text{Ti}_3\text{O}_5 + \text{H}_2 = 3\text{Ti}_2\text{O}_3 + \text{H}_2\text{O}$	Eq.(26)	$119.044 - 0.003T$	35407
$2\text{Ti}_3\text{O}_5 + \text{CH}_4 = 3\text{Ti}_2\text{O}_3 + \text{CO} + 2\text{H}_2$	Eq.(27)	$341.576 - 0.254T$	1343
$\text{Ti}_2\text{O}_3 + \text{H}_2 = 2\text{TiO} + \text{H}_2\text{O}$	Eq.(28)	$180.893 - 0.024T$	7610
$\text{Ti}_2\text{O}_3 + \text{CH}_4 = 2\text{TiO} + \text{CO} + 2\text{H}_2$	Eq.(29)	$400.719 - 0.273T$	1465
$\text{Ti}_2\text{O}_3 + 5\text{CH}_4 = 2\text{TiC} + 3\text{CO} + 10\text{H}_2$	Eq.(30)	$123.675 - 1.042T$	1186

ΔG_f^0 used in these calculations are shown in Table 3.

Meanwhile, the relationship between the Gibbs free energy change and temperature is illustrated in Fig. 2. It is evident that, except for Eq. (4), the initial reaction temperature for most reactions between titanium oxides and H_2 exceeds 2000 K (Fig. 2a and 2c), indicating that these reactions are relatively difficult to initiate. In contrast, the initial reaction temperature range for the reactions between titanium oxides and CH_4 is 1101–1147 K (Fig. 2b and 2d), suggesting that the reaction of TiO_2 with CH_4 occurs more readily.

The abovementioned calculations are based on the reactions occurring under standard atmospheric pressure conditions. In actual experiments, gaseous products are promptly removed along with the carrier gas, leading to a reduction in their partial pressures. Therefore, it is essential to investigate how

the partial pressure of these gaseous products affects the reactions. For simplification, the transformation of TiO_2 to the Magnéli phase is represented by the reaction of TiO_2 to Ti_4O_7 . Based on Eq. (6), the Gibbs free energy change of the reaction and temperature under varying partial pressures of gaseous products were calculated, with the result shown in Table 4.

Fig. 3 reflects the relationships between the Gibbs free energy change and the partial pressure of gaseous products under different temperatures. It is apparent that the Gibbs free energy change decreases when the temperature drops or the partial pressure of gaseous products decreases. Similarly, the initial reaction temperature declines sharply with the decrease in partial pressure. For the same phase transition stage, reactions involving CH_4 occur at a lower temperature than those involving H_2 , indicating that CH_4 is thermodynamically

Table 3 Thermodynamic data (ΔG_f^0) of substances

Substance	$\Delta G_f^0/J \cdot (\text{mol} \cdot \text{K})^{-1}$
TiO_2	$-976986.65 + 484.74T + 1683920.51T^{-1} - 67156788.7T^{-2} - 77.84T \ln(T)$
CH_4	$-348252.33 + 2678.16T + 9.39 \times 10^{-3}T^2 + 2096686.07T^{-1} - 67156788.7T^{-2} + 110598.4 \ln(T) - 40575.91T^{0.5} - 304.93T \ln(T)$
H_2	$-13779.82 - 17.72T - 1.54 \times 10^{-3}T^2 + 147589.949T^{-1} - 2.38 \times 10^{-7}T^3 + 779.44T^{0.5} - 19.83T \ln(T)$
$Ti_{20}O_{39}$	$-19093826.9 + 10248.7T + 28202486.3T^{-1} - 8443.57T^{0.5} - 1050417119T^{-2} - 1609.77T \ln(T)$
$Ti_{10}O_{19}$	$-9324334.79 + 5406.56T + 11363282T^{-1} - 8443.57T^{0.5} - 348849297T^{-2} - 831.39T \ln(T)$
Ti_9O_{17}	$-8347427.08 + 4922.51T + 9679361.2T^{-1} - 8443.57T^{0.5} - 311692519T^{-2} - 753.56T \ln(T)$
Ti_8O_{15}	$-7370431.09 + 4438.51T + 7995440T^{-1} - 8443.57T^{0.5} - 244535742T^{-2} - 675.72T \ln(T)$
Ti_7O_{13}	$-6393300.79 + 3954.56T + 6311520.07T^{-1} - 8443.57T^{0.5} - 177378958T^{-2} - 597.88T \ln(T)$
Ti_6O_{11}	$-5415954.60 + 3470.77T + 4627599.60T^{-1} - 8443.57T^{0.5} - 110222187T^{-2} - 520.04T \ln(T)$
Ti_5O_9	$-4438156.96 + 2987.12T + 2943679.14T^{-1} - 8443.57T^{0.5} - 43075407.1T^{-2} - 442.2T \ln(T)$
Ti_4O_7	$-3459318.88 + 2503.43T + 1259758.59T^{-1} - 8443.57T^{0.5} + 24091372.3T^{-2} - 364.37T \ln(T)$
Ti_3O_5	$-2462333.91 + 1974.08T - 3568008.3T^{-1} - 8443.57T^{0.5} + 353266752T^{-2} - 278.9T \ln(T)$
Ti_2O_3	$-1171154.54 + 6399.42T - 9404192.70T^{-1} - 58419.46T^{0.5} - 730.23T \ln(T)$
TiO	$-558169.7 + 25548T - 8.9 \times 10^{-3}T^2 + 327010.59T^{-1} + 1.1 \times 10^{-8}T^3 - 41.99T \ln(T)$ (α , 298–2500 K) $-553971.14 + 252.16T - 8.9 \times 10^{-3}T^2 + 327074.65T^{-1} + 1.1 \times 10^{-8}T^3 - 41.99T \ln(T)$ (β , 298–2500 K)
TiC	$-207428.36 + 348.26T - 1.56 \times 10^{-3}T^2 + 2635236T^{-1} + 1.07 \times 10^{-7}T^3 - 264300000T^{-2} + 1.2 \times 10^{10}T^{-3} - 53.36T \ln(T)$ (298–900 K) $-207180.25 + 347.63T - 9.8 \times 10^{-4}T^2 + 2605280T^{-1} + 9.09 \times 10^{-8}T^3 - 264300000T^{-2} + 1.2 \times 10^{10}T^{-3} - 53.36T \ln(T)$ (900–1155 K) $-198459.6 + 281.62T - 4.92 \times 10^{-3}T^2 + 1084940T^{-1} + 2.03 \times 10^{-7}T^3 - 264300000T^{-2} + 1.2 \times 10^{10}T^{-3} - 44.31T \ln(T)$ (1155–1941 K) $-323895.23 + 853.45T + 1.14 \times 10^{-2}T^2 + 39262405T^{-1} + 3.04 \times 10^{-7}T^3 - 264300000T^{-2}$ (1941–4000 K)
TiN	$-332270.49 + 457.36T + 1.19 \times 10^{-2}T^2 + 332361.04T^{-1} - 2.04 \times 10^{-6}T^3 - 5877.49 \ln(T) - 70.28T \ln(T)$ (298–1100 K) $-347875.06 + 244.42T - 4.9 \times 10^{-3}T^2 - 846809.02T^{-1} - 40.76T \ln(T)$ (1100–3220 K)
H_2O	$-255475.808 - 15.17T - 7.47 \times 10^{-3}T^2 + 13999.66T^{-1} + 9.2 \times 10^{-8}T^3 + 1107.27 \ln(T) - 25.78T \ln(T)$ (298–1100 K) $-152152.281 + 164.81T - 8.05 \times 10^{-5}T^2 - 12075583.2T^{-1} + 5947.37T^{0.5} - 83128.2757 \ln(T) - 53.15T \ln(T)$ (1100–4000 K)
CO	$-203680.54 + 609.46T + 3.12 \times 10^{-3}T^2 + 770627.67T^{-1} - 10357.02T^{0.5} + 32063.3157 \ln(T) - 90.75T \ln(T)$
CO_2	$-415578.81 + 642.77T + 2.37 \times 10^{-3}T^2 + 20124.52T^{-1} - 6993.15T^{0.5} + 11004.74 \ln(T) - 103.34T \ln(T)$
C	$20210.98 + 515.67T + 4 \times 10^{-3}T^2 - 412784.99T^{-1} - 4096.06T^{0.5} + 1100795.94T^{-2} - 61.18T \ln(T)$ (298–1000 K) $-13835.85 + 176.4T - 4.79 \times 10^{-4}T^2 + 1441704.16T^{-1} - 158.77T^{0.5} - 24.78T \ln(T)$ (1000–6000 K)

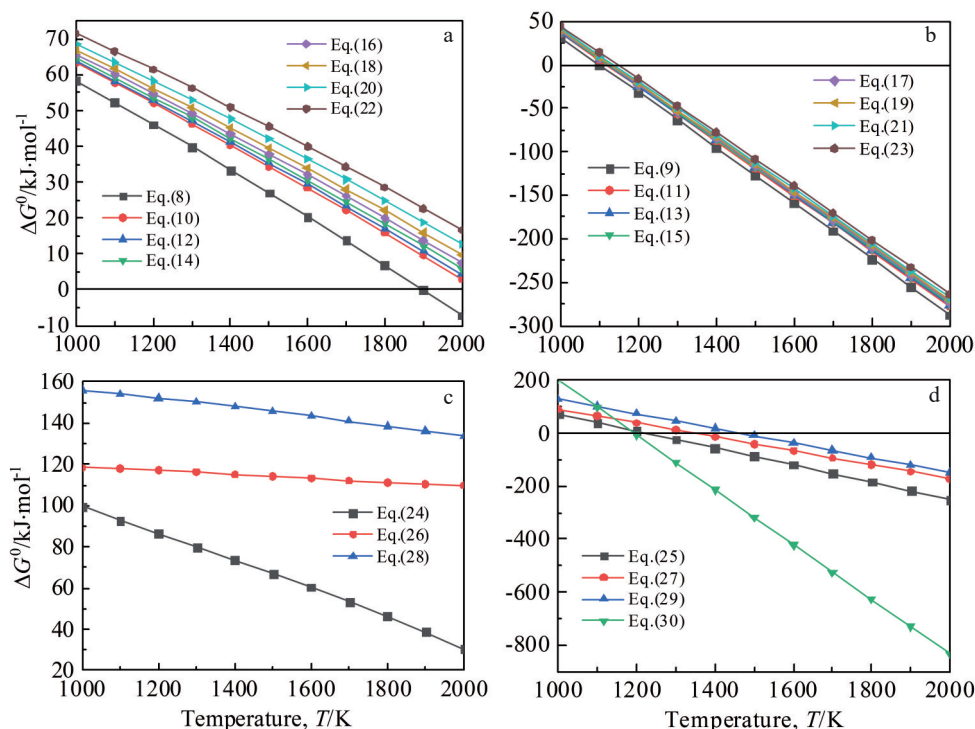


Fig.2 Relationships between standard Gibbs free energy change of Eq.(8–30) and temperature

beneficial to the reduction.

In industrial process, the operating pressure of the reactor ranges from 2×101 kPa to 4×101 kPa. Reactions have been calculated under different system pressures. Changes in system pressure do not affect the reactions involving H_2 ; therefore, only the reactions involving CH_4 are considered, with the results presented in Table 5 and Fig.4. The calculations demonstrate that an increase in system pressure impedes the reduction process, causing the initial reaction temperature to rise progressively.

3.2 Equilibrium phase diagram of TiO_2 in CH_4 - H_2 system

The phase equilibrium of TiO_2 in a CH_4 - H_2 system with varying gas composition is illustrated in Fig.5. As the quantity of reducing gas increases, TiO_2 is initially transformed into the Magnéli phase (Ti_nO_{2n-1} , $n \geq 4$), followed by the Ti_3O_5 phase, and ultimately transformed into a solid solution phase $Ti(C, O)$ composed of TiC and TiO . Additionally, solid carbon is deposited and coexists with titanium oxides at relatively low temperatures. With higher CH_4 concentrations in the gas mixture, the zone where the $Ti(C, O)$ solid solution exists independently, as well as the region where the $Ti(C, O)$ coexist with Ti_3O_5 shifts towards the area with a lower gas/ TiO_2 molar ratio, indicating a reduced total gas requirement for the formation of $Ti(C, O)$. This suggests that the reduction efficiency of titanium oxides is improved with increasing the CH_4 content.

3.3 Solid phase composition of TiO_2 - CH_4 - H_2 system

The TiO_2 -(8vol% CH_4 -92vol% H_2) system was analyzed at various temperatures, and the results are presented in Fig.6. It can be observed that TiO_2 is progressively reduced to the

Magnéli phase and Ti_3O_5 , and ultimately forms a $Ti(C, O)$ solid solution. Notably, at 1173 K, Ti_4O_7 , rather than Ti_3O_5 , is directly transformed into the $Ti(C, O)$ solid solution and cannot be fully reduced even with 50 mol gas. When the temperature exceeds 1373 K, the titanium oxides are entirely converted into the $Ti(C, O)$ solid solution. Thus, an appropriate increase in reaction temperature positively influences the formation of the $Ti(C, O)$ solid solution. As the temperature decreases, solid C is more likely to precipitate in conditions of lower gas partial pressure. In other words, at lower temperatures, methane gas adsorbed on the surface of TiO_2 is more prone to decomposition and generation of solid C. According to Ref.[32–33], C formed under these conditions exhibits excellent activity, enabling the reduction of TiO_2 at lower temperatures.

Fig. 7a illustrates the amount of gas required for the initial and complete formation of the $Ti(C, O)$ solid solution at various temperatures. It is observed that as the reaction temperature increases from 1173 K to 1473 K, the amount of gas required for the initial formation of the $Ti(C, O)$ solid solution decreases from 8.1 mol to 3.4 mol, while the amount required for its complete formation decreases from 48.0 mol to 23.9 mol.

The contents of carbon and oxygen in the $Ti(C, O)$ solid solution are crucial indicators of the deoxidation degree of titanium oxides. Fig. 7b depicts the change in TiC content within the $Ti(C, O)$ solid solution relative to the gas/ TiO_2 molar ratio at different temperatures. When the gas/ TiO_2 molar ratio exceeds 23.9, the TiC concentration in the solid solution rises with increasing the gas content. The turning point of the TiC content aligns with the disappearance of Ti_3O_5 .

Table 4 Gibbs free energy change of titanium oxides reacting with CH₄-H₂ under different product partial pressures

Reaction	$P_{\text{H}_2\text{O}}$ or $P_{\text{CO}}/\times 101 \text{ kPa}$	$\Delta G/\text{kJ}\cdot\text{mol}^{-1}$	$T_{\text{initial}}/\text{K}$
$4\text{TiO}_2+\text{H}_2=\text{Ti}_4\text{O}_7+\text{H}_2\text{O}$	1	$123.168-0.052T$	2360
	10^{-1}	$123.168-0.071T$	1727
	10^{-2}	$123.168-0.090T$	1361
	10^{-3}	$123.168-0.109T$	1124
	10^{-4}	$123.168-0.129T$	957
$4\text{TiO}_2+\text{CH}_4=\text{Ti}_4\text{O}_7+\text{CO}+2\text{H}_2$	1	$345.759-0.303T$	1140
	10^{-1}	$345.759-0.322T$	1073
	10^{-2}	$345.759-0.341T$	1013
	10^{-3}	$345.759-0.361T$	958
	10^{-4}	$345.759-0.380T$	910
$3\text{Ti}_4\text{O}_7+\text{H}_2=4\text{Ti}_3\text{O}_5+\text{H}_2\text{O}$	1	$172.077-0.071T$	2427
	10^{-1}	$171.980-0.090T$	1908
	10^{-2}	$171.884-0.109T$	1572
	10^{-3}	$171.788-0.128T$	1337
	10^{-4}	$171.691-0.148T$	1162
$3\text{Ti}_4\text{O}_7+\text{CH}_4=4\text{Ti}_3\text{O}_5+\text{CO}+2\text{H}_2$	1	$393.339-0.323T$	1218
	10^{-1}	$393.289-0.342T$	1150
	10^{-2}	$393.182-0.361T$	1088
	10^{-3}	$393.096-0.380T$	1033
	10^{-4}	$393.000-0.399T$	984
$2\text{Ti}_3\text{O}_5+\text{H}_2=3\text{Ti}_2\text{O}_3+\text{H}_2\text{O}$	1	$119.044-0.003T$	35407
	10^{-1}	$119.044-0.022T$	5289
	10^{-2}	$119.044-0.042T$	2858
	10^{-3}	$119.044-0.061T$	1958
	10^{-4}	$119.044-0.080T$	1489
$2\text{Ti}_3\text{O}_5+\text{CH}_4=3\text{Ti}_2\text{O}_3+\text{CO}+2\text{H}_2$	1	$341.576-0.254T$	1343
	10^{-1}	$341.576-0.273T$	1249
	10^{-2}	$341.576-0.393T$	1167
	10^{-3}	$341.576-0.311T$	1096
	10^{-4}	$341.576-0.331T$	1032
$\text{Ti}_2\text{O}_3+\text{H}_2=2\text{TiO}+\text{H}_2\text{O}$	1	$180.893-0.024T$	7610
	10^{-1}	$180.682-0.043T$	4220
	10^{-2}	$180.471-0.062T$	2918
	10^{-3}	$180.261-0.081T$	2228
	10^{-4}	$180.050-0.100T$	1802
$\text{Ti}_2\text{O}_3+\text{CH}_4=2\text{TiO}+\text{CO}+2\text{H}_2$	1	$400.719-0.273T$	1465
	10^{-1}	$400.509-0.292T$	1369
	10^{-2}	$400.298-0.311T$	1285
	10^{-3}	$400.087-0.330T$	1210
	10^{-4}	$399.876-0.349T$	1143
$\text{Ti}_2\text{O}_3+5\text{CH}_4=2\text{TiC}+3\text{CO}+10\text{H}_2$	1	$123.675-1.042T$	1186
	10^{-1}	$123.643-1.099T$	1124
	10^{-2}	$123.611-1.157T$	1068
	10^{-3}	$123.580-1.215T$	1017
	10^{-4}	$123.549-1.273T$	971

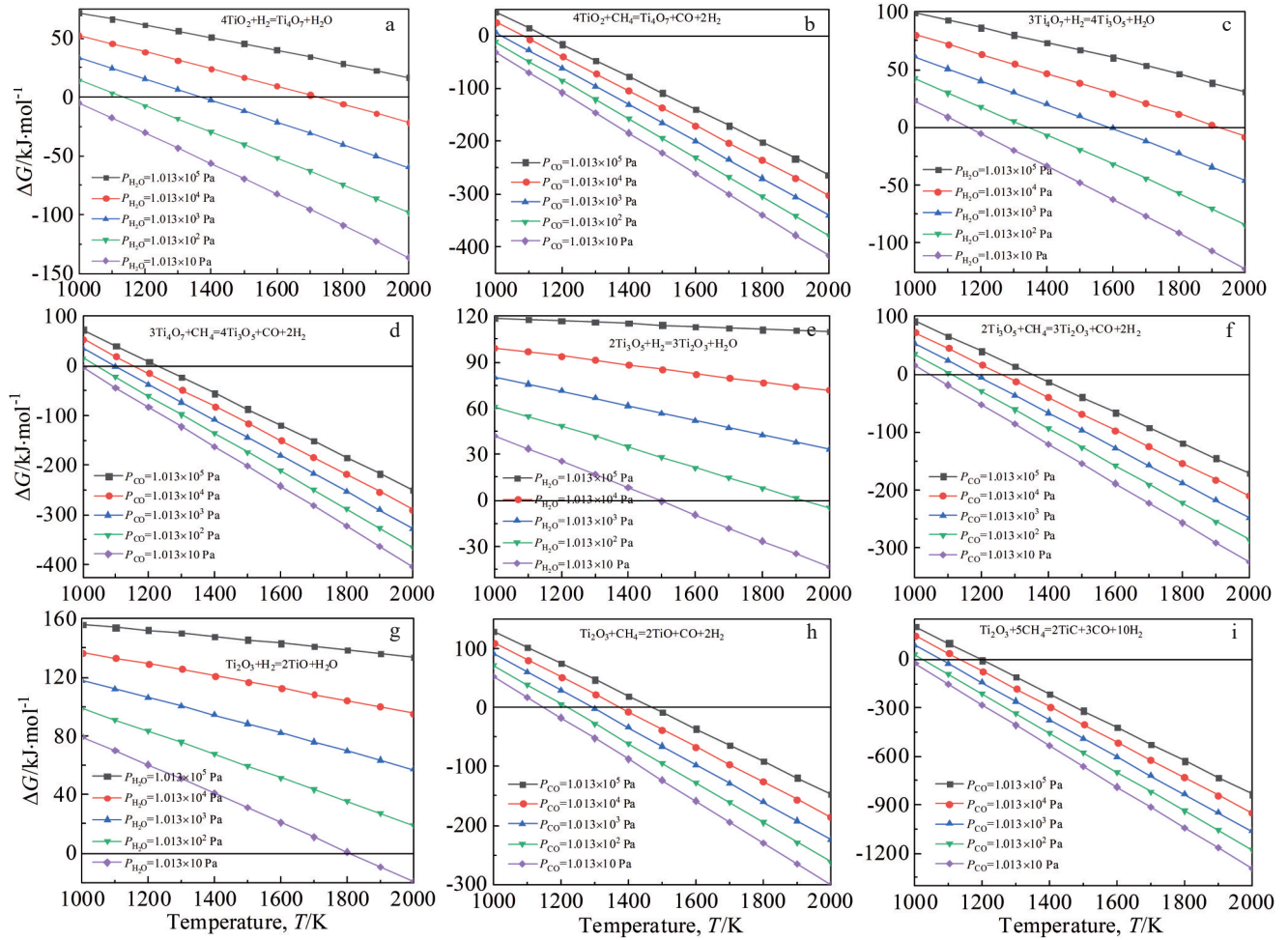


Fig.3 Relationships between Gibbs free energy change and temperature under different partial pressures of gaseous products

Table 5 Gibbs free energy change for reactions of titanium oxides with a $\text{CH}_4\text{-H}_2$ gas mixture under varying system pressures

Reaction	$P/\times 101\text{ kPa}$	$\Delta G/\text{kJ}\cdot\text{mol}^{-1}$	$T_{\text{initial}}/\text{K}$
$4\text{TiO}_2+\text{CH}_4=\text{Ti}_4\text{O}_7+\text{CO}+2\text{H}_2$	1	$354.759-0.303T$	1140
	2	$354.759-0.292T$	1185
	3	$354.759-0.285T$	1213
	4	$354.759-0.280T$	1234
$3\text{Ti}_4\text{O}_7+\text{CH}_4=4\text{Ti}_3\text{O}_5+\text{CO}+2\text{H}_2$	1	$394.992-0.322T$	1228
	2	$394.992-0.310T$	1274
	3	$394.992-0.303T$	1302
	4	$394.992-0.299T$	1323
$2\text{Ti}_3\text{O}_5+\text{CH}_4=3\text{Ti}_2\text{O}_3+\text{CO}+2\text{H}_2$	1	$341.576-0.254T$	1343
	2	$341.576-0.243T$	1407
	3	$341.576-0.236T$	1447
	4	$341.576-0.231T$	1477
$\text{Ti}_2\text{O}_3+\text{CH}_4=2\text{TiO}+\text{CO}+2\text{H}_2$	1	$403.743-0.275T$	1469
	2	$403.743-0.263T$	1533
	3	$403.743-0.257T$	1573
	4	$403.743-0.252T$	1603
$\text{Ti}_2\text{O}_3+5\text{CH}_4=2\text{TiC}+3\text{CO}+10\text{H}_2$	1	$1242.435-1.039T$	1196
	2	$1242.435-0.993T$	1251
	3	$1242.435-0.966T$	1286
	4	$1242.435-0.947T$	1312

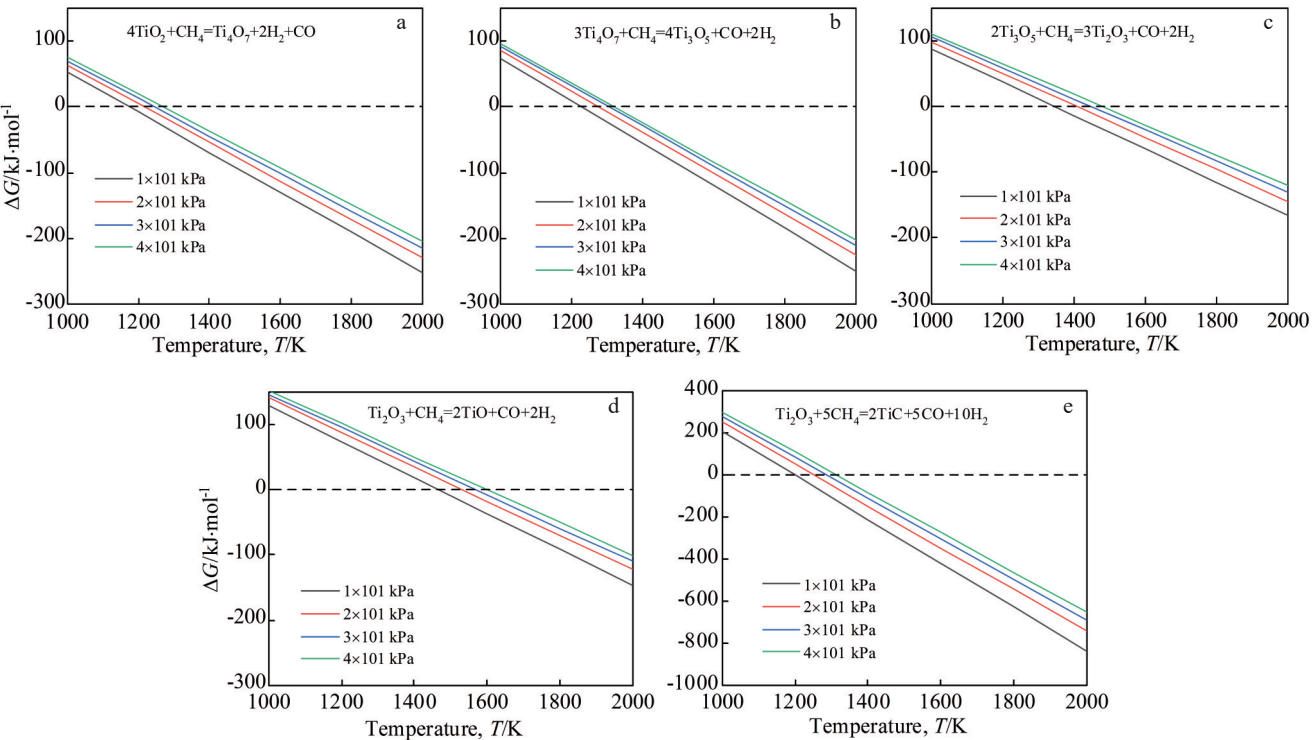


Fig.4 Relationships between Gibbs free energy change of titanium oxides and temperature in CH₄-H₂ gas mixture under varying system pressures

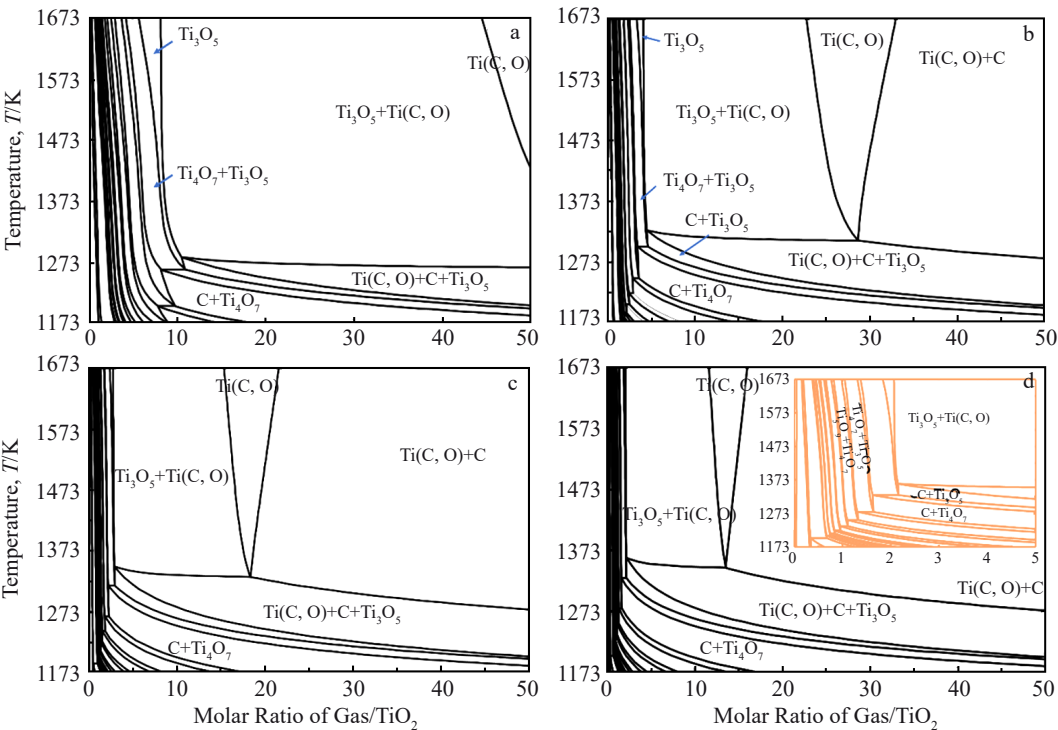


Fig.5 Equilibrium phase diagrams in different gas composition of TiO₂-(CH₄-H₂) systems: (a) TiO₂-(CH₄)_{0.04}(H₂)_{0.96}, (b) TiO₂-(CH₄)_{0.08}(H₂)_{0.92}, (c) TiO₂-(CH₄)_{0.12}(H₂)_{0.88}, and (d) TiO₂-(CH₄)_{0.16}(H₂)_{0.84}

in the phase equilibrium calculations. Once all titanium oxides in the system are transformed into the Ti(C, O) solid solution, TiO is further converted to TiC by CH₄, causing the molar fraction of TiC in the solid solution to increase with the rising gas content.

3.4 Change of reaction enthalpy

The equilibrium between TiO_2 and the CH_4 - H_2 gas mixture in an open system is analyzed, with the calculation conditions detailed in Table 6. To achieve the complete carbonization of TiO_2 , the reaction was divided into 1000 steps, where 0.1 mol

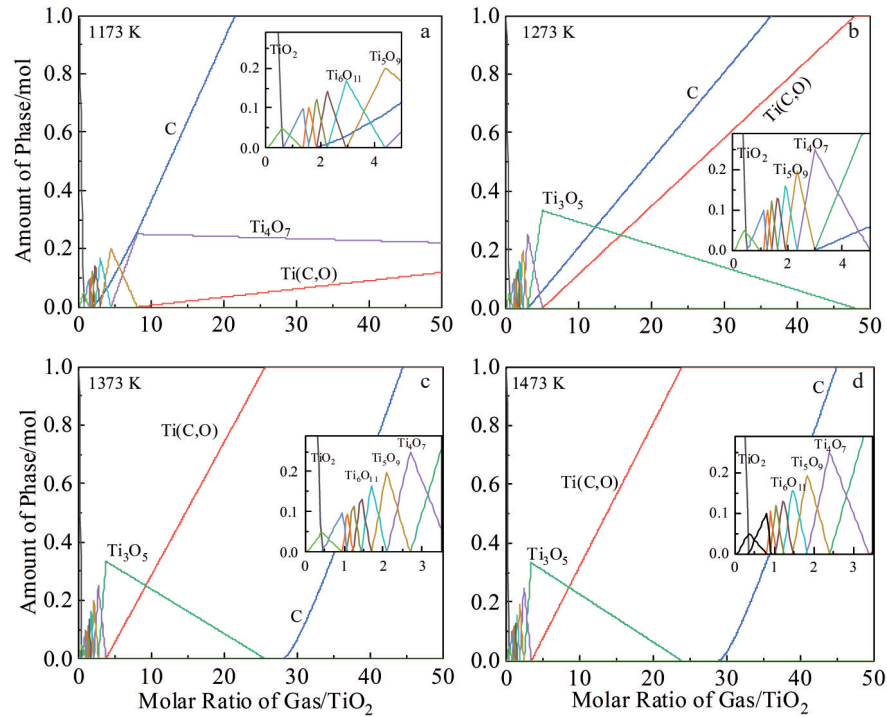


Fig.6 Solid phase composition at different temperatures in TiO_2 -(8vol% CH_4 -92vol% H_2) open system: (a) 1173 K, (b) 1273 K, (c) 1373 K, and (d) 1473 K

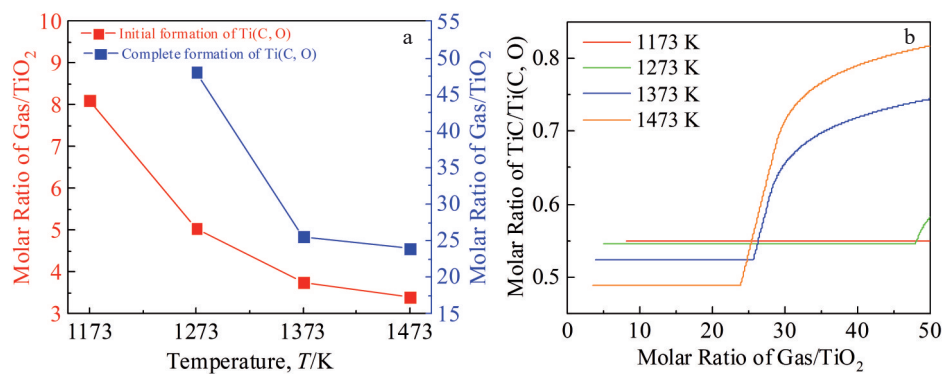


Fig.7 Initial and complete formation points of Ti(C, O) (a) and content variation of TiC in Ti(C, O) (b) in TiO_2 -(8vol% CH_4 -92vol% H_2) open system

Table 6 Calculation conditions of TiO_2 with CH_4 - H_2 gas mixture in open system

No.	$\text{CH}_4/\%$	$\text{H}_2/\%$	$T/^\circ\text{C}$	$P_{\text{total}}/\times 101 \text{ kPa}$
1	8	92	1000	1
2			1100	
3			1200	

reactant gas was introduced in each step. The heat capacity data for each substance in the system are presented in Table 7, which were sourced from the FactSage 8.0 databases (FactPS and FToxid).

As illustrated in Table 8, the amount of gas required for the complete carbonization of 1 mol TiO_2 at 1000, 1100, and 1200 $^\circ\text{C}$ is 48.00, 25.75, and 24.00 mol, respectively. The energy consumption during the reaction process was

calculated and is depicted in Fig.8. This includes the reaction enthalpy of the system at the target temperature and the sensible heat required to heat the substances to the target temperature. The changes in reaction enthalpy at 1000, 1100, and 1200 $^\circ\text{C}$ are 787, 623, and 600 kJ, respectively, highlighting that the reduction process is endothermic.

In practical applications, reactants are typically preheated to a specific temperature using waste heat, which provides a

Table 7 Thermodynamic data of substances during the carbonitriding process of TiO₂

Substance	$C_p/J\cdot(\text{mol}\cdot\text{K})^{-1}$
TiO ₂	$77.83-3367841T^{-2}+4.0294\times10^8T^{-3}$
CH ₄	$304.93-0.0188T-10143.98T^{-0.5}+110598.4T^{-1}-4193372T^{-2}$
H ₂	$19.82+3\times10^{-3}T+1.43\times10^{-6}T^2+194.86T^{-0.5}-295179.9T^{-2}$
Ti ₂₀ O ₃₉	$1609.77-2110.89T^{-0.5}-56404973T^{-2}+6.3025\times10^9T^{-3}$
Ti ₁₀ O ₁₉	$831.4-2110.89T^{-0.5}-22726564T^{-2}+2.273\times10^9T^{-3}$
Ti ₉ O ₁₇	$753.55-2110.89T^{-0.5}-19358722T^{-2}+1.87\times10^9T^{-3}$
Ti ₈ O ₁₅	$675.71-2110.89T^{-0.5}-15990881T^{-2}+1.47\times10^9T^{-3}$
Ti ₇ O ₁₃	$597.88-2110.89T^{-0.5}-12626040T^{-2}+1.06\times10^9T^{-3}$
Ti ₆ O ₁₁	$520.04-2110.89T^{-0.5}-9255199.2T^{-2}+6.61\times10^8T^{-3}$
Ti ₅ O ₉	$442.2-2110.89T^{-0.5}-5887358.3T^{-2}+2.58\times10^8T^{-3}$
Ti ₄ O ₇	$364.37-2110.89T^{-0.5}-2519517.2T^{-2}+1.44\times10^8T^{-3}$
Ti ₃ O ₅	$158.99+0.0502T$
Ti ₂ O ₃	$169.96-750.22T^{-0.5}+1609648.9T^{-2}-1.56\times10^9T^{-3}$
TiO	$41.99+0.0178T-6.64\times10^{-8}T^2-654021.18T^{-2}$
TiC	$53.35+0.0019T+5.45\times10^{-7}T^2-5210560T^{-2}$ (900–1155 K)
	$44.31+0.0098T-1.22\times10^{-6}T^2-2169880T^{-2}$ (1155–1941 K)
TiN	$70.28-0.0024T+1.22\times10^{-5}T^2-5877.49T^{-1}-664722.08T^{-2}$ (298–1100 K)
	$40.76+0.0098T+1693618T^{-2}$ (1100–3220 K)
H ₂ O	$25.78+0.015T-5.52\times10^{-7}T^2+1107.27T^{-1}-27999.3T^{-2}$ (298–1100 K)
H ₂ O	$53.15+1.61\times10^{-4}T-1486.84T^{-0.5}-83128.27T^{-1}+2.41\times10^7T^{-2}$ (1100–4000 K)
CO	$44.09+22893.91T^{-1}-11633086T^{-2}-687.27T^{-0.5}$
CO ₂	$103.34-0.0047T-1748.29T^{-0.5}+11004.74T^{-1}-40249T^{-2}$
C	$61.18-0.008T-1024T^{-0.5}+825570T^{-2}-6604775.7T^{-3}$ (298–1000 K)
	$24.78+9.59\times10^{-4}T-39.69T^{-0.5}-2883408.3T^{-2}$ (1000–6000 K)

Table 8 Amount of gas required for complete carbonization of TiO₂ with CH₄-H₂ gas mixture

No.	CH ₄ /%	H ₂ /%	T/°C	Gas required/mol
1			1000	48
2	8	92	1100	25.75
3			1200	24

portion of heat to the reaction system. Assuming that H₂ and solids are preheated to 900 °C while methane remains unheated due to low-temperature pyrolysis, the adjusted energy consumption is also presented in Fig. 8. The total energy required for the complete carbonization of 1 mol TiO₂ at 1000, 1100, and 1200 °C is 1159, 925, and 977 kJ, respectively. Under these conditions, the total energy

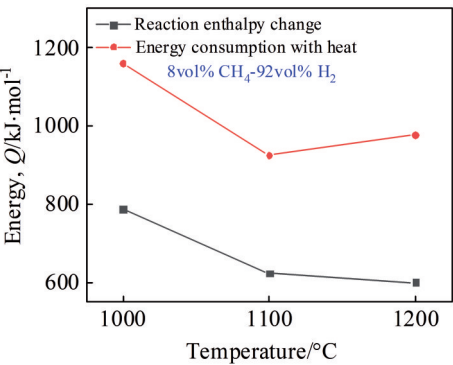


Fig.8 Energy consumption during the reduction process of TiO₂ in CH₄-H₂ gas mixture

consumption for producing 1 t of Ti(C, O) at 1100 °C , considering raw material heating, is 12.17 GJ, which is equivalent to the energy of 415.39 kg standard coal.

4 Conclusions

1) Within the CH₄-H₂ system, the reaction between TiO₂ and H₂ is more difficult to initiate than that between TiO₂ and CH₄. Increasing the CH₄ concentration or raising the reaction temperature can decrease the total gas demand and heat required for the formation of Ti(C, O). Furthermore, the initial reaction temperature decreases with a reduction in partial pressure of gaseous products.

2) TiO₂ is initially transformed into the Magnéli phase, subsequently into the Ti₃O₅ phase, and ultimately into the solid solution phase Ti(C, O). Appropriately elevating the reaction temperature facilitates the formation of the Ti(C, O) solid solution, thereby reducing gas consumption and preventing excessive carbon deposition.

3) Under the conditions of 1100 °C and a gas mixture composed of 8vol% CH₄-92vol% H₂, the enthalpy change and total energy consumption for the complete carbonization of 1 mol of TiO₂ are 623 and 925 kJ, respectively.

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CH₄-H₂混合气体还原二氧化钛的热力学研究

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摘 要: 针对钛及碳化钛制备这一全球关注的重要课题, 开发了一种基于CH₄-H₂混合气体的新型TiO₂还原工艺, 并对其中存在的热力学行为、相平衡和能耗进行了研究。结果表明, 在CH₄-H₂混合气氛下, TiO₂的还原过程呈现出独特的逐步转化特征, 其反应路径遵循从TiO₂到Ti(C, O)的演变规律, 过程中可观察到Magnéli相(Ti_nO_{2n-1})和Ti₃O₅等低价氧化物作为重要的中间相存在。与传统的纯CH₄还原体系相比, H₂的引入显著增加了反应难度, 这一现象可能与H₂对表面碳沉积的抑制作用有关。在能量消耗方面, 获得了具有重要指导意义的数值: 在标准条件下, 1000 °C时完全碳化反应的能耗为1159 kJ/mol, 当温度升至1100 °C时能耗显著降低至925 kJ/mol, 而继续升温至1200 °C时却出现能耗回升至977 kJ/mol的反常现象, 这可能与高温下气相平衡的移动和副反应增加有关。

关键词: TiO₂; TiC_xO_y; 还原碳化; 热力学行为; 能量消耗

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